

Factoring Polynomials: Test Review

Greatest Common Factor

**** First step for all factoring methods

1. Find GCF of all terms $4a^2b^2$
2. Factor (divide) the GCF from each term

$$\frac{24a^3b^2}{4a^2b^2} - \frac{4a^2b^2}{4a^2b^2} - \frac{16a^2b^4}{4a^2b^2}$$

$$4a^2b^2(6a - 1 - 4b^2)$$

Factor by Grouping

<p>Type 1:</p> <ol style="list-style-type: none"> 1. All terms share a common factor 2. Factor the common factor from each term 	$3(x+y) + a(x+y)$ $(x+y)(3+a)$
<p>Type 2: (4 terms)</p> <ol style="list-style-type: none"> 1. Group the 1st two terms and the last two terms. 2. Factor out the GCF from each grouping Notice: Both have the same factor now 3. Factor out the common term 	$(a^2b + 3a^2) + (2b + 6)$ $a^2(b+3) + 2(b+3)$ $(b+3)(a^2 + 2)$

Factoring a Trinomial: Leading Coefficient is 1: $x^2 + bx + c$

<ol style="list-style-type: none"> 1. Find 2 numbers (n_1 and n_2) that MULTIPLY to c and ADD to b 2. List the factors if needed 3. Factor into two binomials $(x + n_1)(x + n_2)$ 	$x^2 + 12x + 20$ $(x+10)(x+2)$
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$$x^2 + 2x - 35$$

$$(x+7)(x-5)$$

$$x^2 - 15x + 56$$

$$(x-7)(x-8)$$

Factoring a Trinomial: Leading Coefficient not 1: $ax^2 + bx + c$

Trial and Error

1. Factors of a need to be the coefficients of the binomials $(a_1x + n_1)(a_2x + n_2)$
2. Factors of c will be the constants n_1, n_2
3. Guess and check

Factor by Grouping

1. Multiply $a \cdot c$
2. Find two numbers (n_1 and n_2) that MULTIPLY to $a \cdot c$ and ADD to b
3. Split up the bx term into $n_1x + n_2x$ creating four total terms
4. Use Factor By Grouping: Group first two terms and last two terms
5. Factor out GCF of each group.
6. Factor out the common factor

$$(2x^2) + 7x + 5$$

$$(2x+5)(x+1)$$

$$\begin{array}{c} \text{---} \\ 5x \\ 2x \\ \text{---} \\ \text{" } 7x \end{array}$$

$$2x^2 + 9x + 4$$

$$(2x+1)(x+4)$$

$$4x^2 - 21x - 18$$

$$(4x+3)(x-6)$$

Mult to
-168

Add to
-17

$4x^2 - 17x - 42$ $(4x^2 - 24x) + (7x - 42)$ $4x(x - 6) + 7(x - 6)$ $(x - 6)(4x + 7)$	$15x^2 + 7x - 4$ $(5x + 4)(3x - 1)$														
$10x^2 - 11x - 6$ $10x^2 + 4x - 15x - 6$ $2x(5x + 2) - 3(5x + 2)$ $(5x + 2)(2x - 3)$ <table border="1" data-bbox="584 630 779 882"> <thead> <tr> <th>P: -60</th> <th>S: -11</th> </tr> </thead> <tbody> <tr><td>1, -60</td><td>59 X</td></tr> <tr><td>2, -30</td><td>-28 X</td></tr> <tr><td>3, -20</td><td>-17 X</td></tr> <tr><td>4, -15</td><td>-11 ✓</td></tr> <tr><td>5, -12</td><td>-7 X</td></tr> <tr><td>6, -10</td><td>-4 X</td></tr> </tbody> </table>	P: -60	S: -11	1, -60	59 X	2, -30	-28 X	3, -20	-17 X	4, -15	-11 ✓	5, -12	-7 X	6, -10	-4 X	<p>GCF</p> $6x^2 - 21x - 45$ $3(2x^2 - 7x - 15)$ $3(2x + 3)(x - 5)$
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1, -60	59 X														
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Special Factoring

<p>Difference of Squares: $a^2 - b^2$</p> <ol style="list-style-type: none"> 1. Square root $a^2 = a$ 2. Square root $b^2 = b$ 3. $(a + b)(a - b)$ $196 - x^2$ $(14 + x)(14 - x)$	$x^2 - 49$ $(x + 7)(x - 7)$ $81y^2 - 100x^2$ $(9y + 10x)(9y - 10x)$
<p>Perfect Square Trinomials</p> <ol style="list-style-type: none"> 1. First term is a perfect square 2. Last term is a perfect square 3. Middle term is twice the first times last 	$x^2 - 10x + 25$ $(x - 5)^2$

$A^2 + 2AB + B^2 = (A + B)(A + B)$ $= (A + B)^2$ $A^2 - 2AB + B^2 = (A - B)(A - B)$ $= (A - B)^2$	$9x^2 + 72x + 144$ $(3x + 12)^2$
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Multiple Techniques

<ol style="list-style-type: none"> 1. Make to check for other factors after using each technique. 2. Often times using one method will turn unveil another factorable situation. 3. The problem isn't complete unless it is fully factored. 	$y^4 - 16$ $\text{DoS: } \underbrace{(y^2 - 4)}_{\text{DoS}}(y^2 + 4)$ $(y + 2)(y - 2)(y^2 + 4)$
$2x^3 - 8x$ $\text{GCF: } 2x(x^2 - 4)$ $\text{DoS: } 2x(x + 2)(x - 2)$	$x^4 - 1$ $\text{DoS: } (x^2 + 1)(x^2 - 1)$ $\text{DoS: } (x^2 + 1)(x + 1)(x - 1)$

SOLVE the following equations (you have to determine which method to use....)		
$x^2 - 3x = 10$ $-10 \quad -10$ $x^2 - 3x - 10 = 0$ $(x - 5)(x + 2) = 0$ $x - 5 = 0 \quad x + 2 = 0$ $\boxed{x = 5} \quad \boxed{x = -2}$	$6x^2 + 11x - 2 = 0$ $(6x - 1)(x + 2) = 0$ $6x - 1 = 0 \quad x + 2 = 0$ $\boxed{x = \frac{1}{6}} \quad \boxed{x = -2}$	$x^2 = 100$ $x^2 - 100 = 0$ DoS $(x + 10)(x - 10) = 0$ $\boxed{x = -10} \quad \boxed{x = 10}$
$8x^2 - 14x = -3$ $8x^2 - 14x + 3 = 0$ $(2x - 3)(4x - 1) = 0$ $2x - 3 = 0 \quad 4x - 1 = 0$ $\frac{2x}{2} = \frac{3}{2} \quad \frac{4x}{4} = \frac{1}{4}$ $\boxed{x = \frac{3}{2}} \quad \boxed{x = \frac{1}{4}}$	$6x^2 = 7x$ $6x^2 - 7x = 0$ $x(6x - 7) = 0$ $\boxed{x = 0} \quad 6x - 7 = 0$ $\boxed{x = \frac{7}{6}}$	$x^2 = 6x - 8$ $x^2 - 6x + 8 = 0$ $(x - 4)(x - 2) = 0$ $\boxed{x = 4} \quad \boxed{x = 2}$

Practice:

$15x^3 + 9x^2$ $3x^2(5x + 3)$	$-6x^4y^2 + 18x^2y - 24xy$ $-6xy(x^3y - 3x + 4)$
$(3ax + 6ay + 4x + 8y)$ $(3a)(x + 2y) + 4(x + 2y)$ $(x + 2y)(3a + 4)$	$(2ac + 4ax - 5c - 10x)$ $2a(c + 2x) - 5(c + 2x)$ $(c + 2x)(2a - 5)$
$9x^2 - 16y^4$ <p>DoS</p> $(3x - 4y^2)(3x + 4y^2)$	$2xy^2z^3 - 18x^3z$ <p>GCF:</p> $2xz(y^2z^2 - 9x^2)$ <p style="text-align: center;">DoS</p> $2xz(yz + 3x)(yz - 3x)$
$3x^6 - 27y^6$ <p>GCF:</p> $3(x^6 - 9y^6)$ <p>DoS:</p> $3(x^3 + 3y^3)(x^3 - 3y^3)$	$x^2 - 7x + 12$ $(x - 3)(x - 4)$

$$x^2 - 4x - 12$$

$$(x-6)(x+2)$$

$$12x^3 - 5x^2 - 3x$$

$$x(12x^2 - 5x - 3)$$
$$x(4x-3)(3x+1)$$

$$-4x^2 + 23x + 6$$

$$-(4x^2 - 23x - 6)$$
$$-((4x^2 - 24x) + (x - 6))$$
$$-(4x(x-6) + 1(x-6))$$
$$-(x-6)(4x+1)$$

$$4x^2 - 18x + 14$$

$$2(2x^2 - 9x + 7)$$
$$2(2x-7)(x-1)$$

20. A baseball is hit with an initial velocity of 80 feet per second. Ignoring the height of the baseball player, how long does it take for the ball to hit the ground? Use $h(t) = -16t^2 + 80t$.

$$h=0$$

$$0 = -16t^2 + 80t$$
$$0 = -16t(t-5)$$

$$t=0$$
$$x$$

$$t=5$$

$$\boxed{5 \text{ sec}}$$

21. A cannonball is shot with an initial velocity of 55 feet per second. Ignoring the height of the cannon, how long does it take for the cannon to hit the ground? Use $h(t) = -16t^2 + 55t$

$$h=0$$

$$0 = -16t^2 + 55t$$
$$0 = -t(16t - 55)$$
$$t=0$$

$$\boxed{t = \frac{55}{16}}$$