

## Factoring Word Problems HW

1. The number of books per shelf in a bookcase is one less than nine times the number of shelves. If the bookcase contains 140 books, find the number of shelves.

*Let  $x = \#$  of shelves*

$$\frac{140}{x} = 9x - 1$$

$$140 = x(9x - 1) \quad -140$$

$$0 = 9x^2 - x - 140$$

$$9x^2 - 36x + 35x - 140 = 0$$

$$9x(x - 4) + 35(x - 4) = 0$$

$$(x - 4)(9x + 35) = 0$$

$$\boxed{x = 4} \quad x = -\frac{35}{9} \times$$

2. The combined area of a square and a rectangle is 225 square yards. The length of the rectangle is eight times the width of the rectangle, and the length of a side of the square is the same as the width of the rectangle. Find the dimensions of the square and the rectangle.

*Let  $w =$   
width of  
rectangle*

$$w \begin{array}{|c|} \hline w \\ \hline \end{array} + w \begin{array}{|c|} \hline 8w \\ \hline \end{array} = 225$$

$$A_1 = w^2$$

$$A_2 = 8w^2$$

$$w^2 + 8w^2 = 225$$

$$9w^2 = 225$$

$$9w^2 - 225 = 0$$

$$9(w^2 - 25) = 0$$

$$9(w + 5)(w - 5) = 0$$

$$w = -5 \quad \boxed{w = 5}$$

$$\times \quad 5 \times 5 \quad 40 \times 5$$

3. Suppose that we want to find two consecutive integers such that the sum of their squares is 613. What are they?

*Let  $x =$  first number*

*$x + 1 =$  second number*

$$x^2 + (x + 1)^2 = 613$$

$$x^2 + x^2 + 2x + 1 = 613$$

$$2x^2 + 2x - 612 = 0$$

$$2(x^2 + x - 306) = 0$$

$$2(x + 18)(x - 17) = 0$$

$$x = -18 \quad | \quad x = 17$$

$$\boxed{-18, -17} \quad | \quad \boxed{17, 18}$$